
MÉTODOS DE INTEGRACIÓN

TABLA DE INTEGRALES INMEDIATAS / COMPOSICIÓN DE FUNCIONES

$p \neq 1$	$\int x^p dx = \frac{x^{p+1}}{p+1} + C$	$\int u^p(x)u'(x) dx = \frac{u^{p+1}(x)}{p+1} + C$
	$\int \frac{1}{x} dx = \ln x + C$	$\int \frac{u'(x)}{u(x)} dx = \ln u(x) + C$
	$\int e^x dx = e^x + C$	$\int e^{u(x)}u'(x) dx = e^{u(x)} + C$
	$\int a^x dx = \frac{a^x}{\ln(a)} + C$	$\int a^{u(x)}u'(x) dx = \frac{a^{u(x)}}{\ln(a)} + C$
	$\int \text{sen}(x) dx = -\text{cos}(x) + C$	$\int \text{sen}(u(x))u'(x) dx = -\text{cos}(u(x)) + C$
	$\int \text{cos}(x) dx = \text{sen}(x) + C$	$\int \text{cos}(u(x))u'(x) dx = \text{sen}(u(x)) + C$
	$\int \text{senh}(x) dx = \text{cosh}(x) + C$	$\int \text{senh}(u(x))u'(x) dx = \text{cosh}(u(x)) + C$
	$\int \text{cosh}(x) dx = \text{senh}(x) + C$	$\int \text{cosh}(u(x))u'(x) dx = \text{senh}(u(x)) + C$
	$\int \frac{1}{\text{cos}^2(x)} dx = \tan(x) + C$	$\int \frac{1}{\text{cos}^2(u(x))}u'(x) dx = \tan(u(x)) + C$
	$\int \frac{-1}{\text{sen}^2(x)} dx = \cot(x) + C$	$\int \frac{-1}{\text{sen}^2(u(x))}u'(x) dx = \cot(u(x)) + C$
	$\int \frac{1}{\text{cosh}^2(x)} dx = \tanh(x) + C$	$\int \frac{1}{\text{cosh}^2(u(x))}u'(x) dx = \tanh(u(x)) + C$
	$\int \frac{1}{\sqrt{1-x^2}} dx = \text{arc sen}(x) + C$	$\int \frac{1}{\sqrt{1-u^2(x)}}u'(x) dx = \text{arc sen}(u(x)) + C$
	$\int \frac{-1}{\sqrt{1-x^2}} dx = \text{arc cos}(x) + C$	$\int \frac{-1}{\sqrt{1-u^2(x)}}u'(x) dx = \text{arc cos}(u(x)) + C$
	$\int \frac{1}{1+x^2} dx = \text{arctan}(x) + C$	$\int \frac{1}{1+u^2(x)}u'(x) dx = \text{arctan}(u(x)) + C$
	$\int \frac{1}{\sqrt{x^2+1}} dx = \text{argsenh}(x) + C$	$\int \frac{1}{\sqrt{u^2(x)+1}}u'(x) dx = \text{argsenh}(u(x)) + C$
	$\int \frac{1}{\sqrt{x^2-1}} dx = \text{argcosh}(x) + C$	$\int \frac{1}{\sqrt{u^2(x)-1}}u'(x) dx = \text{argcosh}(u(x)) + C$
$\text{Si } x < 1$	$\int \frac{1}{1-x^2} dx = \text{argtanh}(x) + C$	$\int \frac{1}{1-u^2(x)}u'(x) dx = \text{argtanh}(u(x)) + C$
$\text{Si } x > 1$	$\int \frac{1}{1-x^2} dx = \text{argcotanh}(x) + C$	$\int \frac{1}{1-u^2(x)}u'(x) dx = \text{argcotanh}(u(x)) + C$

CAMBIO DE VARIABLE

$$\int f(x) dx = \int f(g(t))g'(t) dt$$

INTEGRACIÓN POR PARTES

$$\int u dv = uv - \int v du$$

INTEGRACIÓN DE FUNCIONES TRIGONOMÉTRICAS E HIPERBÓLICAS

En la mayoría de estas integrales deben tenerse en cuenta las distintas relaciones trigonométricas e hiperbólicas. Las principales son:

$$\operatorname{sen}^2(x) = \frac{1 - \cos(2x)}{2}$$

$$\operatorname{cos}^2(x) = \frac{1 + \cos(2x)}{2}$$

$$\operatorname{senh}^2(x) = \frac{\cosh(2x) - 1}{2}$$

$$\operatorname{cosh}^2(x) = \frac{\cosh(2x) + 1}{2}$$

$$\operatorname{sen}^2(x) + \operatorname{cos}^2(x) = 1$$

$$\operatorname{cosh}^2(x) - \operatorname{senh}^2(x) = 1.$$

INTEGRACIÓN DE FUNCIONES IRRACIONALES

- $\int R(x, \sqrt{a^2 - x^2}) dx \implies x = a \operatorname{sen}(t) \longrightarrow dx = a \operatorname{cos}(t) dt$
- $\int R(x, \sqrt{a^2 + x^2}) dx \implies x = a \operatorname{senh}(t) \longrightarrow dx = a \operatorname{cosh}(t) dt$
- $\int R(x, \sqrt{x^2 - a^2}) dx \implies x = a \operatorname{cosh}(t) \longrightarrow dx = a \operatorname{senh}(t) dt$